

PRESSURE IN SLIDE JOURNAL PLANE BEARING BY LAMINAR UNSTEADY OIL FLOW

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Abstract

This paper shows results of numerical solutions a modified Reynolds equation for laminar unsteady oil flow in slide journal plane bearing gap. It shows a preliminary analysis of pressure distribution change in the bearing by laminar, unsteady lubrication caused by velocity perturbations of oil flow in the longitudinal direction of a bearing. Described effect can be used as an example of modelling the bearing friction node operations in reciprocating movement during exploitation of engines and machines. Plane crossbar journal bearing occur in ship combustion engine as a crosshead bearing. During modelling crossbar bearing operations in combustion engines, bearing movement perturbations from engine vertical vibrations causes velocity flow perturbations of lubricating oil on the bearing race and on the bearing slider in the longitudinal direction. Engine forced vertical vibrations frequency and crankshaft forced torsional vibrations is determined by shaft rotational speed, engine cylinder number and by engine type. This solution example applies to isothermal bearing model with infinity length. Lubricating oil used in this model has Newtonian properties and dynamic viscosity in dependence on pressure. Results are presented in the dimensionless hydrodynamic pressure diagrams.

Keywords: journal plane bearing, lubrication, unsteady laminar oil flow, pressure distribution

1. Introduction

Presented subject matter apply to unsteady laminar flows, [1, 4, 5] where modified Reynolds number Re^* is smaller or equal to 2. This flows are also determine by Taylor number Ty which is smaller or equal to 41,1. Laminar and unsteady flow of lubricant factor may occur during periodic or randomness non-periodic load perturbation. This kind of perturbation can occur during transient states of machines, but mostly during starts and stops. Presented work analyse change of oil lubricating flow perturbation in longitudinal direction on the slide plane and on the radial race of slide bearing. Plane bearing can be used as a work model of bearing friction node in kinematic pair in translational motion as an example the crosshead bearing of slow-speed engine. Reynolds equation system for unsteady, laminar Newtonian oil flow in the cylinder radial bearing is presented in work [1] and in the plane slide bearing in work [3]. Stationary model of plane journal bearing lubrication is presented in work [2]. Velocity flow perturbations of lubricating oil on the slide can be caused by axial vibrations during of reciprocating slide motion. Axial vibrations overlay on slide motion and this causes oil velocity perturbation on the slide bearing surface.

Values of the perturbation are proportional to the axial amplitude of perturbation and to forced frequency. Axial vibration in the slide bearing elements can be caused by torsional vibration of the crankshaft. Oil flow velocity perturbations in the axial direction on the bearing race can be caused by axial vibration of the race coming from vertical vibration of the engine. Isothermal bearing model can act as work model of bearing friction node by steady-state conditions of thermal load.

2. Modified Reynolds Equation

Lubricating gap is characterize by following geometric parameters: maximal gap height h_0 , minimal gap height h_e , gap length L and gap width b (fig.1). In presented model the following assumption were made: lubricating gap dimensions along it's width of mating surfaces remain identical. Lubricating gap height after gap length was described in cartesian co-ordinate system by the following dimensionless form:

$$h_1(x_1) = \varepsilon - (\varepsilon - 1)x_1 \quad \text{for } 0 \leq x_1 \leq 1, \quad (1)$$

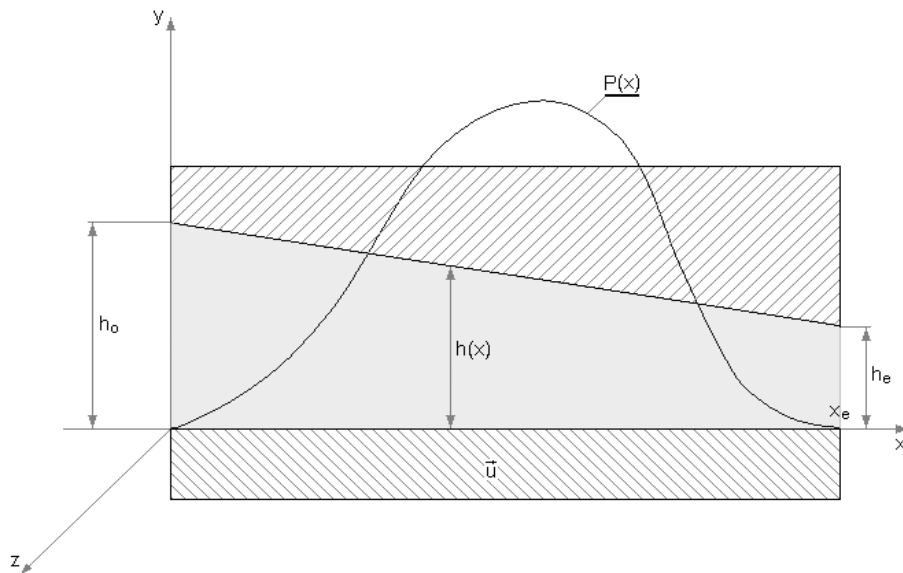


Fig. 1. Geometry schema of the slide journal plate bearing gap

Dimensionless values [2], [3] that characterize lubricating gap are: length coordinate x_1 , gap height coordinate h_1 and gap convergence coefficient ε :

$$h_1 = \frac{h}{h_e}; \quad x_1 = \frac{x}{L}; \quad \varepsilon = \frac{h_0}{h_e}, \quad (2)$$

In considered model we assume small unsteady disturbances and in order to maintain the laminar flow, oil velocity V_i^* and pressure p_1^* are total of dependent quantities \tilde{V}_i ; \tilde{p}_1 and independent quantities V_i ; p_1 from time [3],[5] according to equation (3).

$$\begin{aligned} V_i^* &= V_i + \tilde{V}_i & i &= 1,2,3 \\ p_1^* &= p_1 + \tilde{p}_1 \end{aligned} \quad (3)$$

Unsteady components of dimensionless oil velocity and pressure we [4] in following form of infinite series:

$$\begin{aligned} \tilde{V}_i(x_1; y_1; z_1; t_1) &= \sum_{k=1}^{\infty} V_i^{(k)}(x_1; y_1; z_1) \exp(jk\omega_0 t_0 t_1) & i &= 1,2,3 \\ \tilde{p}_1(x_1; z_1; t_1) &= \sum_{k=1}^{\infty} p_1^{(k)}(x_1; z_1) \exp(jk\omega_0 t_0 t_1), \end{aligned} \quad (4)$$

where:

ω_0 – angular velocity perturbations in unsteady flow,
 $j = \sqrt{-1}$ imaginary unit.

Reynolds equation describing dimensionless total pressure p_1^* in the lubricating gap of a plane journal bearing [3] by unsteady, laminar, isothermal, Newtonian flow together with axial velocity perturbations V_{10} on the race surface and V_{1h} on the slide. Velocity perturbation V_{30} along bearing width on the race and V_{3h} on the slide also occur in this model, as follows:

$$\begin{aligned} & \frac{\partial}{\partial x_1} \left\{ \frac{h_1^3}{\eta_{1B} e^{Kp_1}} \left[\frac{\partial p_1^*}{\partial x_1} - K(p_1^* - p_1) \frac{\partial p_1}{\partial x_1} \right] \right\} + \frac{1}{L_1^2} \frac{\partial}{\partial z_1} \left\{ \frac{h_1^3}{\eta_{1B} e^{Kp_1}} \left[\frac{\partial p_1^*}{\partial z_1} - K(p_1^* - p_1) \frac{\partial p_1}{\partial z_1} \right] \right\} = \\ & = 6 \frac{\partial h_1}{\partial x_1} + \frac{1}{2} \rho_1 \text{Re}^* n \left\{ \frac{\partial}{\partial x_1} \left[\frac{h_1^3}{\eta_{1B} e^{Kp_1}} (V_{10} + V_{1h}) \right] + \frac{1}{L_1^2} \frac{\partial}{\partial z_1} \left[\frac{h_1^3}{\eta_{1B} e^{Kp_1}} (V_{30} + V_{3h}) \right] \right\} \sum_{k=1}^{\infty} A_k + \quad (5) \\ & - 6 \left\{ \frac{\partial}{\partial x_1} [h_1 (V_{10} + V_{1h})] + \frac{1}{L_1^2} \frac{\partial}{\partial z_1} [h_1 (V_{30} + V_{3h})] - 2 \left(V_{1h} \frac{\partial h_1}{\partial x_1} + \frac{1}{L_1^2} V_{3h} \frac{\partial h_1}{\partial z_1} \right) \right\} \sum_{k=1}^{\infty} B_k. \end{aligned}$$

for $0 \leq x_1 \leq 1$; $0 \leq y_1 \leq h_1$; $-1 \leq z_1 \leq 1$; $0 \leq t_1 \leq t_k$; $p_1^* = p_1^*(x_1; z_1; t_1)$.

Oil vector velocity components in dimension form V_x, V_y, V_z and in dimensionless form V_1, V_2, V_3 are described as follows:

$$V_x = UV_1 \quad V_y = \psi UV_2 \quad V_z = \frac{U}{L_1} V_3, \quad (6)$$

where:

- U - linear velocity of slide bearing,
- L - bearing length,
- ψ - relative play ($10^{-4} \leq \psi \leq 10^{-3}$),
- b - bearing width,
- L_1 - relative bearing width:

$$\psi = \frac{h_e}{L}, \quad L_1 = \frac{b}{L}. \quad (7)$$

Oil dynamic viscosity η in dependence on pressure was taken according to the Barru formula [5] and presented [1] in the dimension form η and in dimensionless form η_1

$$\eta = \eta_0 e^{\alpha(p-p_0)} \approx \eta_0 e^{\alpha p}, \quad \eta_1 = \frac{\eta}{\eta_0} = \exp(\alpha p), \quad (8)$$

where:

- η_0 - Oil dynamic viscosity by atmospheric pressure $p = p_a \approx 0$,
- α - piezocoefficient taking into account viscosity changes in dependence on pressure.

Additional assumptions were made[2]: the dimensionless value for density ρ_1 , pressure p_1 , time t_1 and for remaining coordinates y_1 and z_1 according to the following designation:

$$\begin{aligned} \rho &= \rho_0 \rho_1, & p &= p_0 p_1, & t &= t_0 t_1 \\ z &= b z_1, & y &= h_e y_1, & K &= \alpha p_0 \end{aligned}, \quad (9)$$

Density, pressure and time values with zero indexes are equivalent to basic sizes. Constant value K characterizes dynamic viscosity in dependence on pressure. Pressure p_0 , Reynolds number Re, modified Reynolds number Re^* has the following form [2]:

$$p_0 = \frac{U \eta_0}{\psi^2 L} ; \quad Re = \frac{U \rho_0 h_e}{\eta_0} ; \quad Re^* = \psi Re. \quad (10)$$

Sums of a series $\sum_{k=1}^{\infty} A_k$ and $\sum_{k=1}^{\infty} B_k$ in Reynolds equation (5) were defined in works [1, 3].

In the further numerical analysis relation time was taken into account as a propagation period of axial velocity perturbation of lubricating oil.

$$\sum_{k=1}^{\infty} A_k = \sum_{k=1}^{\infty} \frac{\sin(k \omega_0 t_0 t_1)}{k} = \begin{cases} \frac{\pi - \omega_0 t_0 t_1}{2} & 0 < t_1 < 1, \\ 0 & t_1 = 0; 1 \end{cases}, \quad (11)$$

$$\sum_{k=1}^{\infty} B_k = \sum_{k=1}^{\infty} \frac{\cos(k \omega_0 t_0 t_1)}{k^2} = \frac{1}{4} \left[(\pi - \omega_0 t_0 t_1)^2 - \frac{\pi^2}{3} \right] \quad 0 \leq t_1 \leq 1.$$

In case where oil velocity perturbations are caused by forced vibrations of engine then the number n in equation (5) define multiplication of perturbation frequency ω_0 to angular velocity of engine crankshaft ω .

3. Hydrodynamic pressure

Equation solution (3) for infinity length bearing with assumption that velocity perturbation does not depend on coordinate x_1 can be present [3] in total dimensionless hydrodynamic pressure p_1^*

$$p_1^*(x_1) = p_{1K} - \frac{p_{10}}{1 - Kp_{10}} (V_{10} - V_{1h}) \sum_{k=1}^{\infty} B_k + \frac{x_1}{4\varepsilon^2} \frac{\rho_1 Re^* n}{1 - Kp_{10}} (V_{10} + V_{1h}) \left(\varepsilon + 1 - \frac{\varepsilon + h_1}{h_1^2} \right) \sum_{k=1}^{\infty} A_k +$$

$$+ \frac{3K}{(\varepsilon - 1)^2} \frac{\rho_1 Re^* n}{1 - Kp_{10}} (V_{10} + V_{1h}) \left\{ (x_1 - 1) \ln \varepsilon - \ln h_1 + \frac{1}{\varepsilon + 1} \left[(\varepsilon - 1)(1 - 2x_1) + \frac{\varepsilon}{h_1} - h_1 \right] \right\} \sum_{k=1}^{\infty} A_k. \quad (12)$$

The p_{10} value is a pressure value in the discussed lubricating gap by the steady flow with the constant lubricating oil dynamic viscosity. On the other hand p_{1K} value is a stationary pressure value for viscosity, in dependence on pressure and for discussed form of lubricating gap it was mentioned in work [2]:

$$p_{10} = \frac{6(\varepsilon - 1)(1 - x_1)x_1}{(\varepsilon + 1)(\varepsilon - \varepsilon x_1 + x_1)^2} ; \quad p_{1K} = -\frac{1}{K} \ln |1 - Kp_{10}|, \quad (13)$$

$$\lim_{K \rightarrow 0} p_{1K} = p_{10}.$$

Perturbation pressure \tilde{p}_1 in the unsteady part of the flow can be presented as a difference of total pressure p_1^* and stationary pressure p_{1K} .

On the basis of presented dependences for isothermal bearing model with infinity width, the calculations of hydrodynamic pressure distribution in the lubricating gap were made. In the example calculations the following assumption were made: oil with constant density and value of the expression $n \rho_1 Re^* = 12$, which approximately comply to axial velocity perturbation function in the engine crosshead bearing after the first frequency force from two-stroke, six cylinder engine crankshaft torsional vibration. Hydrodynamic pressure distribution and other pressure parameters are in dependence on lubricating gap convergence coefficient ε [2]. Optimum gap convergence $\varepsilon_{opt} = 1 + \sqrt{2}$ comply to maximal hydrodynamic pressure. Pressure in the optional point of lubricating gap changes due the perturbation time and its distribution along the gap length reach the maximal and minimum values. On the Fig.2 example of the hydrodynamic total pressure distribution along the gap length for bearing with the optimal convergence ε_{opt} and for the convergence $\varepsilon = 1,4$ marked

with numbers 1 and 2 by the constant viscosity ($K=0$) in dependence on pressure ($K=0,25$) marked with thin and thick lines. Maximal pressure distribution were marked with symbols a and the minimal pressure distribution were marked with b. Pressure quantities by stationary flow were marked with broken line.

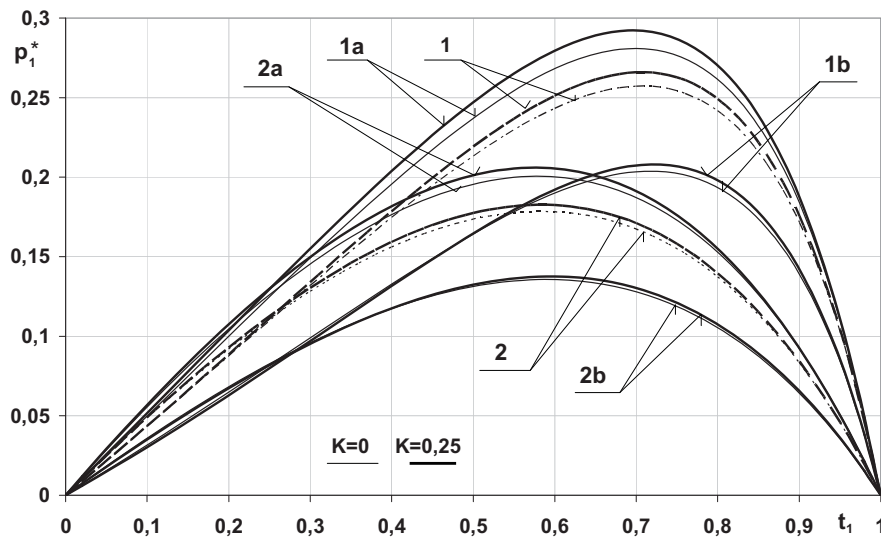


Fig. 2. Total maximal (a) and minimal (b) pressure distributions p_1^* in direction x_1 for ε : 1) $\varepsilon = \varepsilon_{opt}$; 2) $\varepsilon = 1,4$ by velocity perturbations: $V_{10}=0,05$

Unsteady flow on the Fig.2 is caused by axial velocity perturbation only on the bearing race $V_{10}=0,05$. In the case where oil dynamic viscosity depends on pressure then pressure perturbations are higher than in the case where oil has constant viscosity. Pressure perturbation quantity depends on lubricating oil convergence ε and is the maximum for optimal convergence. It apply also to stationary pressure increase in the lubricating gap. Further analysis of pressure distribution were made for gap with optima convergence ($\varepsilon=\varepsilon_{opt}$).

Total pressure distribution along the bearing gap and perturbation pressure distribution in the time function in the optional point on the race surface were analyzed. Numerical calculation results were presented by following axial velocity perturbations:

1. Velocity perturbation on the race $V_{10}=0,05$,
2. Velocity perturbation on the race $V_{10}=0,05$ and on the slide $V_{1h}=0,025$.

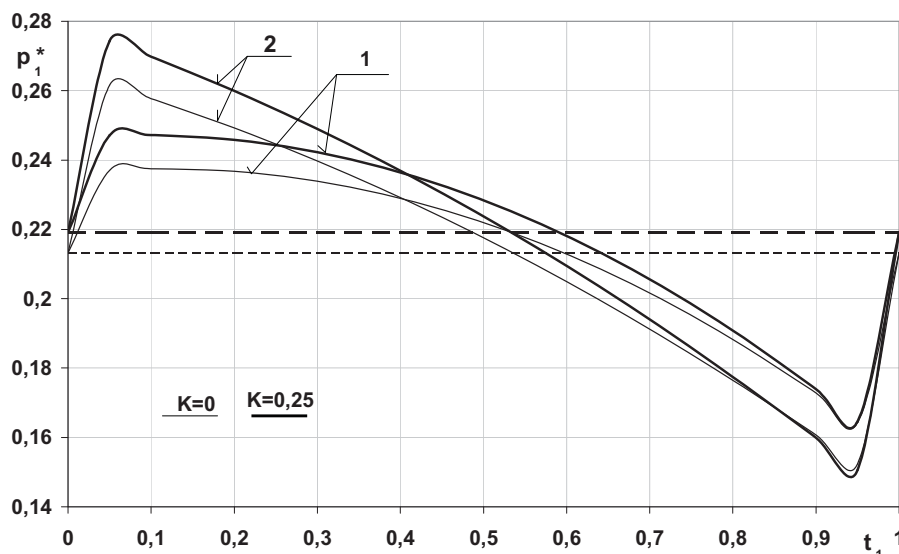


Fig. 3. Pressure distributions p_1^* in place $x_1=0,5$ in the time t_1 by velocity perturbations: 1) $V_{10}=0,05; V_{1h}=0$; 2) $V_{10}=0,05; V_{1h}=0,025$

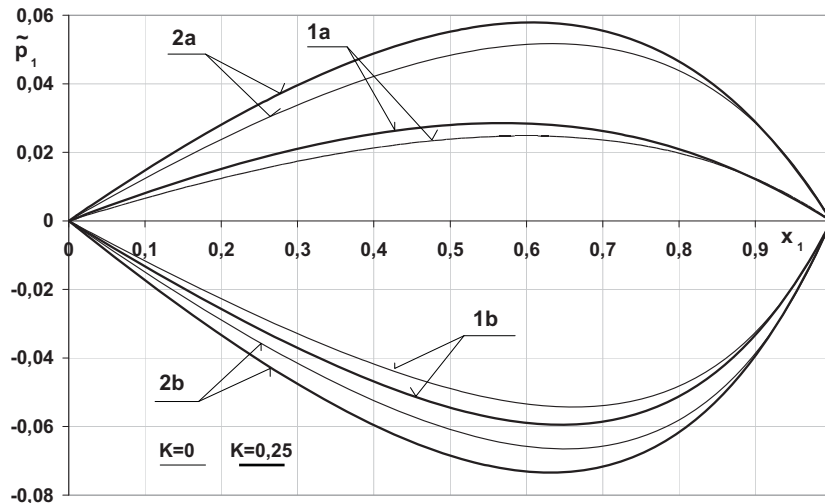


Fig. 4. Unsteady part maximal (a) and minimal (b) pressure distributions \tilde{p}_1 in direction x_1 by velocity perturbations:
 1) $V_{10}=0,05$; $V_{1h}=0$; 2) $V_{10}=0,05$; $V_{1h}=0,025$

Unsteady pressure is changing at the time of velocity perturbation and its course is a function of time and its location along the bearing length. It is the temporary function of a period of velocity perturbation. Total pressure course p_1^* in the point located in the half way of bearing length $x_1=0,5$ on the surface of the race in dimensionless time function is presented on the figure 3 for two different velocity perturbation. Steady pressure is marked with the misfiring line. When the velocity perturbation of oil on the race is harmonious with the slide velocity, the perturbation pressure will increase. In the opposite situation it decreases and the drop is much higher than the rise. It lasts shorter than the half perturbation period. The opposite case is when velocity perturbation takes place on the slide. This case has not been presented on the figure. The periods of drop and rise of pressure are asymmetric in the case of different levels of velocity perturbation. (Figure 3). The level of velocity perturbation is higher for both options when the viscosity depends on the pressure.

The distribution of velocity perturbation \tilde{p}_1 along the gap is changing according to time, giving maximum and minimum pressure in different moments of time. The distribution of maximum and minimum pressure perturbation along the bearing length is presented on the figure 4. for the discussed cases of velocity perturbation of oil flow. Drops in the total pressure are higher than its rises. It applies to the situation when the oil flow is of constant and variable dynamic viscosity. However, the rise of steady pressure as a cause of variable viscosity compensate higher drop and minimum total pressure is changing slightly, as it is shown on the figures 2 and 3.

4. Conclusions

Discussed case of the solution to the Reynolds equation for the unsteady laminar Newtonian flow of lubricating factor allows initial estimation of hydrodynamic pressure distribution and its capacity as a basic operational parameter slide bearing. Unsteady axial velocity perturbation on the race surface and slide has influence on the hydrodynamic pressure distribution of the capacity of the lubricated gap. Pressure changes in the bearing are seasonal and equal to the lasting period of velocity perturbation. The level of changes and its nature depends on the kind of perturbation. The author bears in mind of the number of simplifying assumptions used in the presented model of bearing node and applying to the acceptance of Newtonian oil as well as examining isothermal model of bearing. The presented analytical example applies to the bearing of infinite length, however, the conclusions can be useful for the estimation of the pressure distribution and force with laminar, unsteady lubrication of slide nodes of the finished length. Presented results can be

used as the comparative values in the case of numerical modeling of laminar, unsteady flows of liquids non-Newtonian in lubricating gaps slide journal bearings.

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